## Paper / Subject Code: 29701 / Applied Mathematics - II.

## F.E. SEM - II / CHOICE BASED / MAY 2019 / 09.05.2019

## **Duration – 3 Hours**





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- N.B 1) Question No. 1 is Compulsory.
  - 2) Answer any three questions from remaining questions.
  - 3) Figures to the right indicate full marks.

Q.1 a) Evaluate 
$$\int_0^\infty y^4 e^{-y^6} dy$$
.

- b) Find the circumference of a circle of radius r by using parametric equations of the circle  $x = r\cos\theta$ ,  $y = r\sin\theta$ .
- c) Solve  $(D^2 + D 6)y = e^{4x}$ .
- d) Evaluate  $\int_0^1 \int_{x^2}^{x} xy(x^2 + y^2) dy dx$ .
- e) Solve  $(tany + x)dx + (xsec^2y 3y)dy = 0$ .
- f) Solve  $\frac{dy}{dx} = 1 + xy$  with initial condition  $x_0 = 0$ ,  $y_0 = 0.2$  by Euler's method. Find the approximate value of y at x = 0.4 with h = 0.1.

Q.2 a) Solve 
$$(D^2 - 4D + 3)y = e^x \cos 2x + x^2$$
.

- b) Show that  $\int_0^\infty \frac{\tan^{-1}ax}{x(1+x^2)} dx = \frac{\pi}{2} \log(1+a)$ .
- c) Change the order of integration and evaluate  $\int_0^2 \int_{\frac{x^2}{2}}^{4-x} xy dy dx$ . 8
- Q.3 a) Evaluate  $\iiint x^2yz \, dx dy dz$  throughout the volume bounded by 6 the planes x = 0, y = 0, z = 0 and  $\frac{x}{a} + \frac{y}{b} + \frac{z}{c} = 1$ .
  - b) Find the mass of lamina of a cardioid  $r = a(1 + cos\theta)$ .

    If the density at any point varies as the square of its distance from its axis of symmetry.
  - c) Solve  $(3x+2)^2 \frac{d^2y}{dx^2} + 5(3x+2)\frac{dy}{dx} 3y = x^2 + x + 1$ .

- Q.4 a) Find by double integration the area common to the circles r = 6  $2\cos\theta$  and  $r = 2\sin\theta$ .
  - b) Solve  $\sin 2x \frac{dy}{dx} = y + \tan x$ .
  - c) Solve  $\frac{dy}{dx} = 3x + y^2$  with initial conditions  $y_0 = 1$ , 8  $x_0 = 0$  at at x=0.2 in steps of h=0.1 by Runge Kutta method of fourth order.
- Q.5 a) Evaluate  $\int_0^1 x^5 \sin^{-1} x \, dx$  and find the value of  $\beta\left(\frac{7}{2}, \frac{1}{2}\right)$ .
  - b) The differential equation of a moving body opposed by a force 6 per unit mass of value cx and resistance per unit mass of value  $bv^2$  where x and v are the displacement and velocity of the particle at that time is given by  $v\frac{dv}{dx} = -cx bv^2$ . Find the velocity of the particle in terms of x, if it starts from the rest.
  - c) Evaluate  $\int_0^6 \frac{dx}{1+4x}$  by using i) Trapezoidal ii) Simpsons (1/3)rd 8 and iii) Simpsons (3/8)th rule.
- Q.6 a) Find the volume of the region that lies under the paraboloid z = 6  $x^2 + y^2$  and above the triangle enclosed by the lines y = x, x = 0 and x + y = 2 in the xy plane.
  - b) Change to polar coordinates and evaluate  $\int \int y^2 dx dy$  Over the area outside  $x^2 + y^2 ax = 0$  and inside  $x^2 + y^2 2ax = 0$ .
  - Solve by method of variation of parameters  $\frac{d^2y}{dx^2} + y = \frac{1}{1+\sin x}.$

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